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**U.S. DEPARTMENT OF ENERGY**  
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# END REGION AND CURRENT CONSOLIDATION EFFECTS UPON THE PERFORMANCE OF AN MHD CHANNEL FOR THE ETF CONCEPTUAL DESIGN

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## Abstract

Operating conditions which yielded the peak thermodynamic efficiency (41 percent) for an ETF-size MHD/steam plant were previously identified by considering only the active region (the primary portion for power production) of an MHD channel. In this paper, the efforts of the previous study are extended to include the investigation of the effects of the channel end regions on the overall power generation. Considering these effects the peak plant thermodynamic efficiency is found to be slightly lowered (40.7 percent) and the channel operating point for the peak efficiency is shifted to the supersonic mode (Mach No.,  $M_c \sim 1.1$ ) rather than the previous subsonic operation ( $M_c \sim 0.9$ ). The sensitivity of the channel performance to the B-field, diffuser recovery coefficient, channel load parameter, Mach number, and combustor pressure is also discussed. In addition, methods for operating the channel in a constant-current mode are investigated. This mode of channel operation is highly desirable from the standpoint of simplifying the current and voltage consolidation for the inverter system. This simplification could result in significant savings in the cost of the equipment. The initial results of this study indicate that this simplification is possible, even under a strict Hall field constraint, with reasonable plant thermodynamic efficiency (40.5 percent).

## I. Introduction

Previous studies<sup>1,2</sup> have identified MHD channel configurations and operating conditions which result in peak thermodynamic efficiency of the combined MHD/steam plant. A critical factor in these studies was that the MHD channel was cooled by low pressure, low temperature boiler feedwater. This results in a lowering of the steam plant efficiency with increasing MHD channel heat loss since it reduces the amount of regenerative boiler feedwater heating that can be done within the steam plant itself. In these initial studies, only the active (significantly power producing) region of the channel was considered. This region was taken to extend from a B-field low of 4 tesla at the front of the channel to a B-field low of approximately 3.5 tesla at the rear of the channel (see Fig. 1). However, even though the regions upstream and downstream of the active region do not produce significant amounts of power, they still produce significant voltage which requires voltage isolation. Therefore, these regions require MHD-channel-type construction and hence cooling with low-pressure, low-temperature boiler feedwater with the attendant possibility of a further reduction in overall plant efficiency.

The results presented in this paper apply only to plants of the size of the ETF conceptual design (200 MW<sub>e</sub>) and to MHD channels whose design requirements specify cooling with low-pressure, low-temperature boiler feedwater. The sensitivity of various channel parameters (maximum B-field, dif-

fuser recovery coefficient, generator load parameter, Mach number, and combustor pressure) are examined under the constraints of a maximum axial electric field ( $E_x$ ) of 2.5 kV/m, a maximum transverse electric field ( $E_y$ ) of 4 kV/m, and a maximum transverse current ( $J_y$ ) of 10 kA/m<sup>2</sup>. In addition, the channel performance is investigated using constant current output in various regions of the channel in order to take advantage of possible cost savings for the inverter system under these conditions.<sup>3,4</sup>

## II. Background

The channel analysis is based on a quasi-one-dimensional code.<sup>5</sup> However, in this study the code has been modified to allow the calculation of the voltage drops through the integral boundary layer. This is necessary since the original model is inadequate for the channel end regions. In addition to the voltage-drop calculations, the channel code utilizes tabulated chemical equilibrium properties which are computed separately.<sup>6</sup> This allows a considerable reduction of the required computing time, especially in the region of the boundary layers. The channel code is then combined with an overall system calculation<sup>2</sup> to determine the performance of the MHD/steam plant.

## III. Channel Characteristics

The operating conditions and electrical stress constraints used in this study are given in Table 1. In Ref. 1, the optimal channel had an active length of 12 m. In this study, the end regions of the channel are included by starting the calculations at the 0.5 tesla point and considering the entire length of the channel to be 16 m which results in a B-field of 0.5 tesla at the exit (Fig. 1). At these B-field levels, the Hall electric field at the channel entrance and exit is approximately 10 V/m and 40 V/m, respectively. At these electric field levels, voltage isolation is no longer a serious problem and the construction is that of the nozzle or diffuser which are cooled by intermediate or high-pressure boiler feedwater which does not seriously affect the overall system efficiency.

## IV. Results

Table 2 lists the results for twelve cases all optimized for combustion pressure ( $P_c$ ) and load coefficient ( $K_{min}$ ). These cases are for the ETF conceptual design input power level of 540 MW<sub>t</sub>, an air enrichment level of 30 percent O<sub>2</sub> by volume, and a length of 16 m, as discussed below.

### Base Case

Case 1 is the result of adding the end regions to the initial ETF channel configuration in which only the active region (central 12 m) was considered.<sup>1</sup> In case 1,  $P_c$  and  $K_{min}$  have been readjusted to obtain the peak overall system efficiency for the total length of 16 m. An over-

all efficiency of 40.3 percent was obtained which compares to the 41 percent obtained previously. Axial profiles of  $E_x$ ,  $E_y$ ,  $J_y$ ,  $K$ , MHD power ( $P_{MHD}$ ), and Hall parameter ( $\beta$ ) for this case are plotted in Fig. 2.

#### Variation of Mach Number and Maximum B-Field

The effect of varying the inlet Mach number on the plant overall thermodynamic efficiency is shown in Fig. 3 for peak B-fields of 6 tesla (cases 1-4) and 5 tesla (cases 5-8). It is seen that for the  $B_{max} = 6$  tesla case a maximum efficiency of 40.7 percent is obtained at a supersonic Mach number of 1.1. This compares to a value of 41 percent at a Mach number of 0.9 obtained for the original 12-m channel calculation.<sup>1</sup> The increase in optimum Mach number for the present calculation is primarily the result of the fact that a lower average B-field exists in this longer channel. As was shown in Ref. 1, the lowering of the B-field results in a higher optimum Mach number. This is again born out as can be seen from the results for the  $B_{max} = 5$  tesla cases 5-8 where the maximum efficiency of approximately 40.4 percent occurs at a Mach number of 1.25.

In all of the above cases for  $B_{max} = 6$  tesla, the diffuser pressure recovery coefficient,  $C_D$ , was held constant at 0.46. A sensitivity study was then conducted by considering  $C_D = 0.4$  and 0.55. The result of this variation is shown in cases 9 and 10 of Table 2. It is seen that the sensitivity in the overall efficiency is about  $\pm 0.2$  percent over this range of recovery coefficients.

#### Constant Faraday Current Operation

ETF conceptual design studies have shown that considerable simplification of the consolidation and inverter circuitry can be obtained by operating the generator at constant Faraday current,  $I_y = J_y A_e$ , where  $A_e$  is the effective electrode area. Cases 11 and 12 of Table 2 show the effect upon performance of attempting to operate various regions of the channel in this constant current mode. Because of the direct relation of  $J_y$  to the axial electric field, i.e.,  $J_y \sim \sigma E_x / \beta$ , the current level is in turn limited by the  $E_x$  constraint—especially at the downstream section of the channel where the electrical conductivity ( $\sigma$ ) drops and the Hall parameter ( $\beta$ ) is high. The results of case 11 in which an attempt was made to operate the entire channel at a constant current output of  $I_{y,max} \sim 2.9$  kA/m (where  $I_{y,max}$  is the maximum transverse current/unit length) are shown in Fig. 4. The axial variation of  $I_y$ ,  $J_y$ ,  $E$  and  $\beta$  are depicted on the figure. Nearly one half of the channel can be run at constant current but at  $X \sim 8$  m the Hall field limit is reached.

In an attempt to further simplify the inverter system, i.e., to eliminate the continuously varying current output at the latter half of the channel, a two-level case ( $I_{y,max} \sim 3.0, 2.5$  kA/m; case 12) was investigated. The results are shown in Fig. 5 and are not significantly different from those in Fig. 4. Using two levels of constant current does not extend the length of constant

current appreciably and does not render significant simplification of the current consolidation system over case 11.

Preliminary calculations show that if  $E_{x,max}$  is relaxed to about 3.5 kV/m, almost the whole channel can be controlled at one level of constant current but the plant thermodynamic efficiency drops about one point relative to case 11. Nevertheless, both cases 11 and 12 show reasonable performance for partial constant-current control with a plant thermodynamic efficiency ( $\eta_{th}$ ) of about 40.5 percent.

#### Concluding Remarks

This study of the MHD channel for a 540 MW<sub>th</sub>, ETF-size plant, 16 m long, including the end sections suggests:

1. The best performance is obtained in the supersonic mode, even for  $B_{max} = 6$  tesla ( $\eta \sim 40.7$  percent,  $M_c \sim 1.1$ ).
2. Lowering  $B_{max}$  to approximately 5 tesla does not severely lower the performance ( $\eta_{th} = 40.4$  percent at  $M_c \sim 1.25$ ) and could result in a reduction of the magnet size of up to 40 percent.
3. The overall performance is not too sensitive to diffuser pressure recovery coefficient. For a  $C_D$  range of 0.4 – 0.55, the overall efficiency changes by  $\pm 0.2$  percent.
4. A simplification of the inverter system is possible. Good channel performance ( $\eta_{th} \sim 40.5$  percent) can be obtained using a partial constant-current mode, even under a strict electrical constraint on the Hall field ( $E_{x,max} \sim 2.5$  kV/m). If this constraint could be relaxed to about 3.5 kV/m, the entire channel could be controlled by a constant-current operation; however, the penalty in plant efficiency might not be negligible.

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TABLE 1. - THE OPERATING CONDITIONS AND ELECTRIC STRESS CONSTRAINTS

Thermal input, MW	540
Coal type	Montana Rosebud
Moisture content in coal, percent	5
Oxidizer (O <sub>2</sub> enriched air), vol. percent	30
Oxidizer preheat temperature, °F	1100
Seed, 1 percent-mass, K	K <sub>2</sub> CO <sub>3</sub>
Total flow rate, kg/sec	133
Combustor heat loss, percent	5
Combustor slag rejection, percent	65
Oxygen stoichiometry, percent	90
Poly. eff. of cycle compressor, percent	89.8
Specific power of ASU, kW-hr/ea. ton O <sub>2</sub>	204
Ambient pressure (atm) and temperature (°F)	0.89; 42
B-field	National Magnet Laboratory (NML) preliminary design (Fig. 1)
Axial electric field limit, kV/m	2.5
Transverse electric field limit, kV/m	4.0
Transverse electric current limit, kA/m <sup>2</sup>	10

TABLE 2 - PERFORMANCE OF THE 16-m CHANNEL FOR ETF WITH END REGIONS

(O<sub>2</sub> ~ 30 percent, B<sub>max</sub> ~ 5.6 tesla, M<sub>c</sub> ~ 0.9 ~ 1.35, C<sub>D</sub> ~ 0.4 - 0.55)

Case no.	B <sub>max</sub> , tesla	Mach no	Diffuser coefficient	Combustor pressure, atm	MHD power, MWe	Channel heat loss, Mwt	Cycle compressor power, MW	O <sub>2</sub> compressor power, MW	Bottom cycle input, Mwt	Steam cycle efficiency, percent	Steam cycle output, MWe	Cycle coal input, Mwt	Gross ac power, MWe	Thermal cycle efficiency, percent
1	6	0.9	0.46	4.4	85.06	28.48	21.98	11.62	430.47	38.76	133.25	539.81	217.5	40.29
2		0.95		4.4	86.10	27.79	21.98	11.62	429.13	38.80	133.03	539.21	218.3	40.43
3		1.07		4.4	87.39	25.42	21.98	11.62	428.14	38.96	133.19	539.81	219.7	40.70
4		1.15		4.3	86.29	23.99	21.60	11.62	428.86	39.05	134.23	539.81	219.7	40.69
5	5	1.05	0.55	4.4	81.18	26.18	21.98	11.62	434.35	38.91	135.39	539.81	215.9	39.97
6		1.15		4.2	82.95	24.10	21.31	11.62	431.91	39.05	135.79	539.81	217.9	40.37
7		1.25		4.0	81.39	21.67	20.42	11.62	432.57	39.20	137.20	539.81	218.1	40.40
8		1.35		3.7	77.52	19.56	19.17	11.62	435.20	39.51	140.27	539.81	217.0	40.20
9	6	0.9	0.40	4.5	83.90	28.96	22.36	11.62	432.10	38.71	133.40	539.81	216.4	40.08
10				4.5	87.08	27.90	22.36	11.62	428.82	39.79	132.39	539.81	218.6	40.49
11				4.2	86.26	28.22	21.21	11.62	428.50	38.77	133.30	539.81	218.7	40.51
12				4.2	86.51	27.95	21.21	11.62	428.25	38.79	133.27	539.81	218.9	40.56

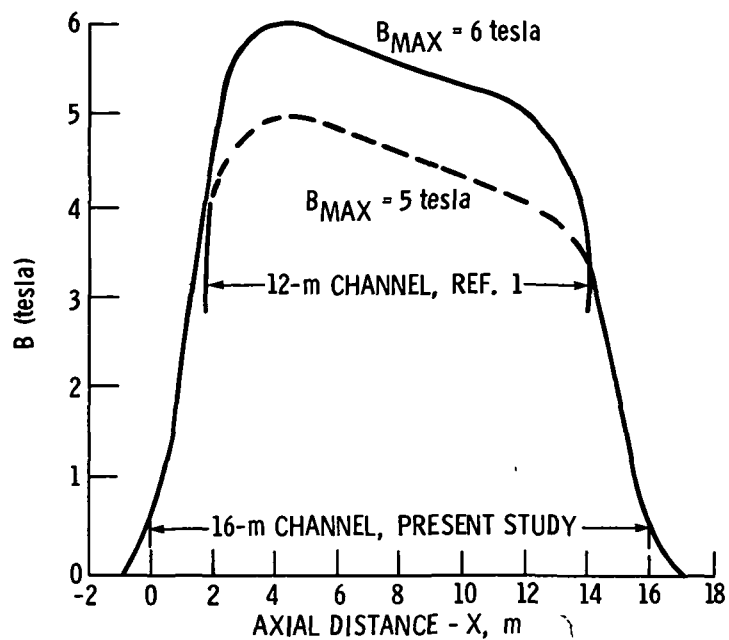


Figure 1. - Axial profile of B-field from National Magnet Laboratory preliminary design for the ETF.

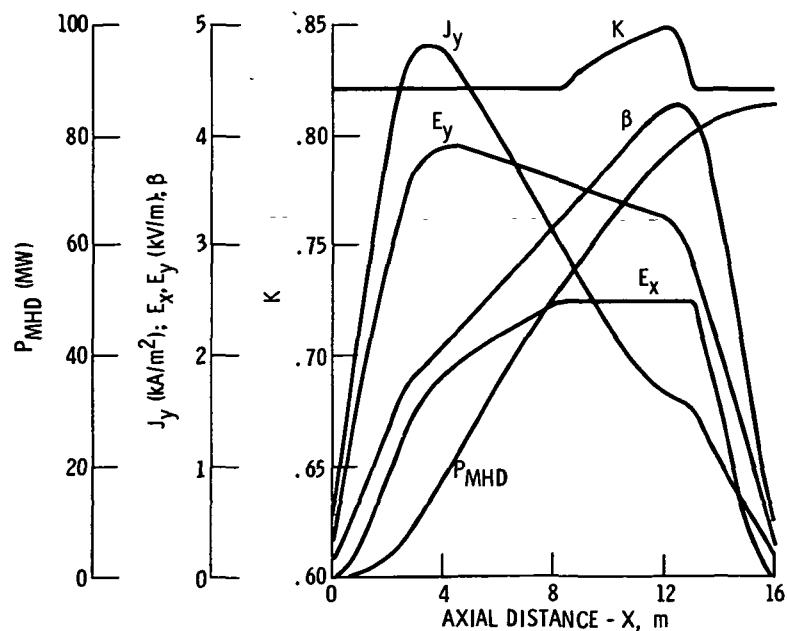


Figure 2. - Axial profiles of  $E_x$ ,  $E_y$ ,  $J_y$ ,  $K$ ,  $P_{MHD}$ , and  $\beta$  for case 1. ( $O_2$  = 30 %-vol.,  $M_c$  = 0.9, 16-m channel.)

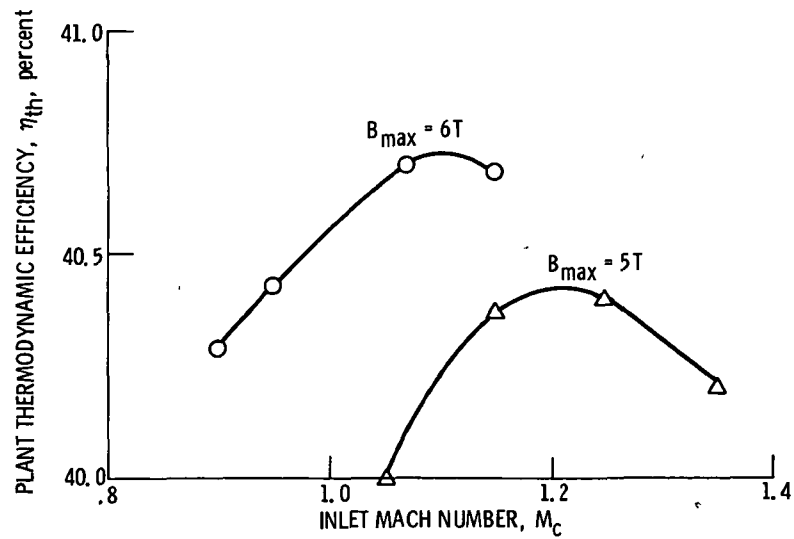


Figure 3. - Thermodynamic efficiency versus Mach number for maximum B-field of 6 tesla and 5 tesla.

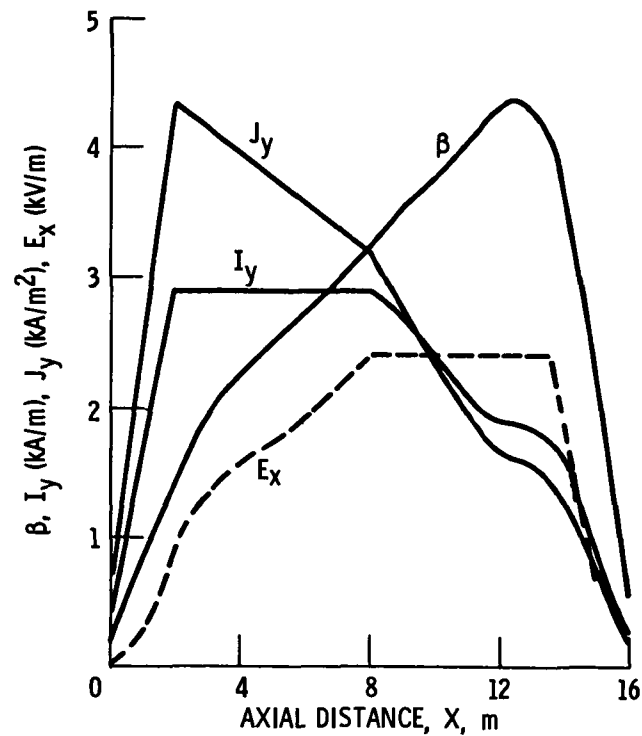


Figure 4. - Axial profiles of  $E_x$ ,  $I_y$ ,  $J_y$ , and  $\beta$  for one-level, constant-current control, case 11. ( $I_{y,max} = 2.9$  kA/m;  $E_{x,max} = 2.5$  kV/m).



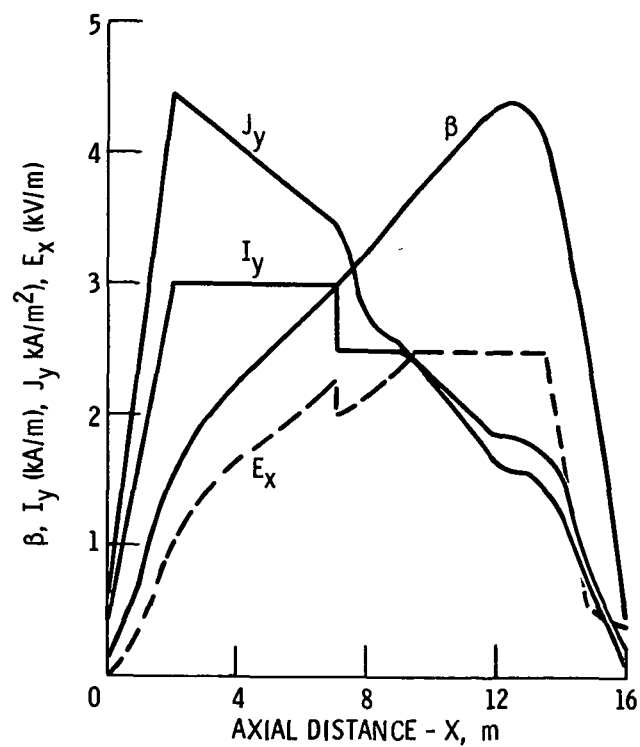


Figure 5. - Axial profiles of  $E_x$ ,  $I_y$ ,  $J_y$ , and  $\beta$  for two-level constant-current control, case 12. ( $I_{y,max} = 3.0/2.5$  kA/m;  $E_{x,max} = 2.5$  kV/m.)

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